SPATIAL PATTERN IN MODELING ELECTRICITY PRICES:
EVIDENCE FROM THE PJM MARKET

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Abstract. This paper analyses the evolution of electricity prices in deregulated market. I formulate a model that takes into account the spatial features of a network of a market. The model is applied to equilibrium electricity spot prices of the PJM market. An empirical analysis indicates that the problem of unobserved spatial correlation in the network can be modeled by the Spatial Error Model providing an additional insight about the spot electricity prices in the PJM market. The topology of the network and the structure of the market are responsible for the spatial correlation, which should not be ignored by careful research.

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Introduction

Worldwide liberalization of the electricity markets – the introduction of competition, opening the electricity markets to new providers, reduction of external inferences – aims to boost competition for generation entities, load serving firms and ancillary services. In deregulated electricity markets, participants can act strategically, thus reduce the transparency of the electricity prices and causing welfare loss. Relationships between prices and operating decisions have been thoroughly and systematically studied in last decade. Analyses of electricity prices in deregulated electricity markets revolve around three main questions: (1) Do electricity markets perform efficiently? (2) What model do prices follow? (3) How important is financial deregulation to market performance? While enhancing competition in electricity markets, the changes have made electricity a traded commodity that is sold and bought through various exchange markets in real time as well as with futures and options, meaning that trading and risk management have become key tools for running a successful business. Moreover, financial regulation of energy markets plays a significant role and is becoming increasingly relevant to the electricity sector as trading continue to develop. Doing business in the new electricity markets therefore requires adequate models of price dynamics that capture the main characteristics and features of electricity prices.

Electricity is not a typical commodity since it cannot be economically stored. This unique feature of electricity is the key determinant of the high volatility of market-clearing prices. Since inventories cannot be stored to smooth supply and demand shocks, generation and consumption have to be continuously balanced in real time, which creates substantial price volatility. Risk associated with real time production and consumption shocks has impeded the conversion of energy market structure from monopolistic to a competitive, efficient form. As the electricity market structure has moved from a monopolistic to an increasingly competitive one, the following changes have occurred in US electrical energy markets:

- Wholesale power markets have grown rapidly in recent years (US Department of Energy Report, 2000)
- Increasing uncertainty of market prices, and consequent development of methods to hedge risk, including the formation of formation of day ahead markets and futures markets (Bessembinder and Lemmon, 2002, Longstaff and Wang, 2002, Routlegde, Seppi and Spatt (2001))
• Improved trading contracts and standards and development of financial transmission rights (PJM annual report 2002, Gibson and Schwartz (1990))

In addition, it seems plausible that volume of trades will continue to grow in the future. Hence, it is likely that with the further elaboration and decentralization of the power market, new trading standards and entirely new energy-related markets may emerge. Together, these factors motivate additional research on electricity markets, price modeling, high-frequency empirical studies, and analysis of the welfare impacts of the structural changes.

This paper addresses the issue of modeling spot prices, because spot prices are one of the key factors in strategic planning and decision support systems of a majority of market players, and are the underlying instrument of a number of electric power derivatives. The goal of the paper is to propose a model for electricity spot price dynamics that takes into account the key characteristics of electricity price formation in the PJM interconnection such as seasonality, weather-dependence, trading in the day-ahead market and spatial attributes of the distribution system.

There is a large and growing literature on electricity markets, their deregulation, efficiency, electricity prices formation and risk management. Recent important theoretical works on electricity spot and forward prices include work by Bessembinder and Lemmon (2002), Routledge, Seppi and Spatt (2001) and Longstaff and Wang (2002). Bessembinder and Lemmon develop an equilibrium model of electricity market for spot and forward prices in a production economy and provide some empirical evidence supporting their model. Routledge, Seppi and Spatt construct a model with rational expectations for electricity prices, assuming that storable commodities such as gas and coal are available to be converted into electricity. While Routledge, Seppi and Spatt (2000) present a theoretical model for general commodities, Escribano, Peaea and Villaplana (2002), and Lucia and Schwartz (2002) focus on energy contracts, Empirical evidence about the forward premium, i.e. difference between the forward and expected spot price, for storable commodities is presented by French (1986), Fama and French (1987), Hazuka (1984).

Electricity is not a typical good since its flow is not easily controlled. Given the grid, injections on the nodes and knowledge of the Kirchhoff’s Current Law, one can only predict electricity flows i.e. accurately estimate the electricity flow distribution within a grid. There is one degree of freedom – injections on some nodes and loads on the other nodes. Changing production and load in different locations can manipulate both the direction and intensity of electricity flows within a given grid. Transmission and distribution lines are the only means by which electricity can be delivered to users. The topology of transmission lines plays a significant role in electricity price formation, since the
pricing mechanism of electricity depends on the ability to deliver at a specified time and place. Therefore, the topology of the grid is a major determinant of electricity prices in all deregulated markets. Although participants in a competitive electricity market act independently, individual behavior does influence the performance of the entire system, because all electricity market participants act simultaneously under the physical constraints of the system and economic constraints of the market.

The effect of simultaneous constraints can be illustrated by an ideal market under Cournot competition. In a market for a homogeneous good, with N producers and fixed demand, the profit-maximizing production of any producer depends on the production of all other participants. In the case of an electricity market, each generating unit’s production depends not only on how much others generate but also on how many transmission lines are available to deliver the product and the capacity and congestion of the lines, which are also affected by the production of all other participants.

The novelty of my approach is the utilization of the spatial feature of the PJM market which is divided into twelve transmission zones. The PJM interconnection’s pricing mechanism and price data availability is designed in such a way as to allow considering each zone as a hypothetical generating unit. Both forward and spot prices are reported for each hypothetical producer hourly. This facilitates a high-frequency empirical analysis taking into account spatial characteristics of the interconnection. Consequently, I assume that the electricity spot price can be represented as a function of its lagged values, the forward price, weather conditions, and demand, which is equal to load. I assume that there is a unique price generating process, but the disturbances are spatially correlated due to the grid topology and the omitted variables problem. My main finding is that the spatial aspect plays an essential role in electricity prices formation and that ignoring the spatial characteristics and the grid topology may cause biased results and vague conclusions.

OVERVIEW OF ELECTRICITY CHARACTERISTICS

Non-storability

The non-storability of electricity makes this commodity special and prevents researchers from using standard methods to analyze electricity market and its performance. Although it is possible to consider electricity to be a storable commodity if the supply stack consists mostly of hydropower generation as in Norway, in the case of thermal generation electricity cannot be considered as a storable commodity. Therefore, reaction to a sudden change in demand will necessarily occur with a time gap that can be significant. In particular, the non-storability of electricity subverts the cost-of-
carry argument and intertemporal arbitrage-based methods, which are used in the classical financial approach to risk assessment and valuation. Since electricity cannot be economically stored, it is necessary to develop specific tools to analyze power markets.

Supply and Demand

Uncertainty about quantity demanded and supply shortages influences price formation in electricity markets. To better understand this, it is essential to disentangle overcapacity and shortage in supply as well as demand weather-dependence and non-receptivity to price changes.

In an economically efficient and unconstrained electricity market, generation units are dispatched according to marginal cost; i.e., it is rational to dispatch first the generating unit with the lowest marginal cost, followed by units with higher marginal cost in merit order. Every generating unit has its minimum production as well as its maximum production, which are determined by both physical and economic considerations. So, the supply curve is relatively smooth and production is elastic in the range between minimum and maximum generation, but after the unit’s capacity ceiling is reached its supply curve becomes vertical. These facts complicate the economic dispatch problem and bring uncertainty to it since demand is not known a priori.

Demand for electricity is affected by different factors such as industrial, commercial and domestic use, which contribute to variation within the day, week and season. Cyclical deviations may be predicted with a high degree of certainty. Nonetheless, some important sources of disturbance such as weather conditions, wind speed, temperature, and humidity make electricity demand highly inelastic. Supply shortages follow unpredicted demand jumps and unexpected generating plant and transmission lines maintenance problems, and so, are not generally foreseen. Innate characteristics of the generating units’ capacity limit, demand insensitivity to price fluctuations, weather-dependence of consumption, complexity of grid network and risk associated with supply-demand balancing -- all contribute significantly to the volatility of electricity prices.

Seasonality

Seasonality is another feature of electricity prices and generation, which fluctuate in response to the variation of demand. Demand shifts and subsequent price movements are primarily influenced by exogenous factors such as weather conditions and economic and domestic activities. Moreover, the non-storability of electricity plays a part in seasonality of electricity prices because it reduces the possibility of a lagged use. For instance, electricity use is low at night and high at noon, but it is not possible to generate electricity at night in order to balance demand increases during the day. There are three kinds of seasonality detected in different studies in electricity prices and load: diurnal, weekly
and annual. Diurnal seasonality can be explained by the large change in consumption between day and night, i.e. peak and off-peak hours. Weekly seasonality comes from differences in industrial activity between work days and weekends. Annual seasonality is related to weather conditions such as the season, temperature, and wind speed.

It is usual to assume that seasonality is generated by deterministic factors. It is possible to demonstrate seasonality without a mathematical formula. Figures 1 and 2 illustrate seasonal patterns in prices and production. Visual examination of the left panel shows that weekly prices display a seasonal pattern over a yearly cycle. The right panel represents intra-day seasonality in prices. Note that load exhibits exactly the same behavior, although it is less volatile than electricity price.

There are also mathematical methods such as Fourier analysis, fast Fourier transform analysis and moving average seasonality analysis, which allow us to detect seasonality problem in continuous, discrete, periodic and even a-periodic series. For discrete and periodic series the Fast Fourier transform is appropriate. Fig. 3 illustrates the frequency spectrum of PJM hourly locational marginal prices and load. In analyzing the spectrum, the daily, weekly and annual frequencies are clearly visible. Lower frequencies for 12, 6, and 3 hours are also observed. However, they do not give any additional information and are simply the resonance of “daily” peak. These peaks for 12 hours, 6, and 3 hours are called harmonics (multipliers of 24) and indicate that data exhibit a 24-hours period but it is not sinusoidal.
Empirical studies show that prices in many electricity markets can be characterized as mean reverting process. For instance, Bhanot (2000), Lucia and Schwartz (2002), and Knittel and Roberts (2001) model electricity prices as a mean-reverting process. That is, electricity prices fluctuate around their mean although the mean itself may evolve over time. It is plausible to assume that the electricity price mean depends on demand, supply and market structure. There are at least two theoretical explanations for the mean reversion phenomenon. First, shifts in demand push prices up, as more expensive generators are called upon in turn and the market moves along the supply curve. Second, since weather evolves as a mean reverting process, and since equilibrium prices are highly affected by demand (which is weather dependent), it is natural to assume that electricity prices exhibit mean reversion. There is a large literature devoted to electricity price formation processes, treated as mean reverting, for instance Knittel and Roberts (2001), Delaloye, Bernezet and Meisser (EGL AG report 2001), Lucia and Schwartz (2001). Although mean reverting models are very attractive, there is also literature describing electricity prices as non-mean reverting. Moreover, the recently developed alternatives to mean reverting and mean reverting with jumps models are non-constant volatility (GARCH/ARCH). For instance, one can find the GARCH models of electricity prices and their derivatives in Escribano, Pena and Villaplana (2002), Longstaff and Wang (2002).

**PJM Market**

The PJM Interconnection is a regional transmission organization (RTO) established in 1997 as the first auction-based market in the USA. The PJM energy market coordinates the continuous buying
and selling of energy in real-time and day-ahead markets, forward and bilateral markets and self-supply. PJM Interconnection ensures production, transmission and the interconnection reliability of the centrally dispatched control area. It establishes and supports the trading rules and standards; facilitates the market-clearing prices; monitor market activities to ensure open and fair access.

PJM coordinates the movement of electricity in all or parts of Delaware, Maryland, New Jersey, Ohio, Pennsylvania, Virginia, West Virginia and the District of Columbia. The PJM interconnection consists of two independent areas: PJM East and PJM West. PJM West is represented by one transmission zone, whereas PJM East is divided into eleven transmission zones. All twelve transmission zones are responsible for security of transmission system, balancing of generation and switching coordination. There are approximately 245 market participants in PJM energy market, including power generators, transmission owners, electricity distributors, and large consumers. Market members fall in four main market sectors: generation-owner, transmission-owner, electric distribution and end-users. Depending on market conditions, each participant from any market sector can be either buyer or seller. However, all sectors have their specific rules and requirements, which must be fulfilled.

The PJM energy market uses a Locational Marginal Pricing model (LMP) that reflects the value of energy at the specific location and times it is delivered. If the lowest-priced electricity can reach all locations (i.e. there is no transmission congestion), prices are the same across all locations. However, if there is transmission congestion, so energy cannot flow freely to certain locations, more expensive generating units have to be dispatched out of merit order to meet demand. As the result, the locational marginal price (LMP) is higher in those locations.

The PJM energy market consists of Real-Time and Day-Ahead markets. The Day-Ahead Market is a forward market in which hourly LMPs are calculated for the next operating day based on demand bids, generation supply bids and scheduled bilateral transactions. The Real-Time Market is a spot market in which current LMPs are calculated every five minutes based on actual system operating conditions. PJM transactions are settled hourly, and both real time and day ahead LMPs are available for each of the twelve transmission zones.

**DATA**

The data consist of hourly Real-Time and Day-Ahead Location Marginal Prices from the PJM market spanning the period of April 1, 2002 to December 31, 2003. For each of the 641 days in the sample, the data sets contain information on hourly real-time LMP ($) for each zone, and the 24 settlement LMP ($) for the day-ahead forward market, where delivery will be made at the respective
hour during next day. The data contain the power delivery (MW) for each day hourly from both PJM-East and PJM-West hubs. The data are provided directly from the PJM website www.pjm.com.

Table 1 reports the summary statistics for the electricity spot and forward prices over the period of April 1, 2002 to December 31, 2003. Both spot and forward prices are quoted in dollars per megawatt hour, $/MWh. As shown in Table 1, both the average spot and forward prices do not vary much among the zones. However, standard deviations are smaller for forward prices, meaning that forward prices are less volatile. Median spot prices are lower than mean spot prices, indicating a rightward skewness of the spot price's distribution. Although the same pattern can be observed in the forward prices, the differences between mean and median spot prices are smaller than the differences between mean and median forward prices. Minimum of the spot prices is higher than minimum of the forward prices in absolute values. And the spot peak prices are much bigger than the forward peak prices.

Tables 2 and 3 present the summary statistics for the average hourly spot and forward electricity prices. The average spot prices vary throughout the day, running from a low for the early morning to a high for the peak late afternoon. Both average hourly spot and forward prices clearly exhibit intraday variation. It is interesting that mean forward prices are higher than the mean spot prices during the peak afternoon hours, while median spot prices are almost always lower than median forward prices, indicating that spot prices have a more pronounced upward skewness. Standard deviations are high for afternoon prices for both forward and spot markets, and the standard deviations for the spot prices are always higher than standard deviations for the forward prices. The maximum spot price is about 15 times higher than its mean values during afternoon hours, whereas the maximum forward price is about only 4 times higher than mean values for these hours. This summary of the price statistics demonstrates the key feature of electricity prices: their right-skewed distribution. The model presented in Routledge, Seppi and Spatt (2001) implies the same pattern of skewness.

For Figures 6, 7 and 8, I use the data spanning the period of January 1, 2002 to December 31, 2003 in order to capture annual seasonality as well as daily and weekly seasonality. Two zones are excluded from this analysis since they have operated since April 1, 2002.

Figure 6 shows time series of average over zones electricity spot prices for a representative subset of hour. As it can be seen, there is a considerable time series variation in the spot prices, particularly during peak hours. Figure 7 plots the forward prices for the same subset of hours. The forward prices exhibit similar properties as the spot prices, though they are less volatile.
Hourly electrical load for PJM Eastern and PJM Western hubs measured in gigawatt hours represents electrical usage. Figures 1, 2, 3 and 8 illustrate that the load data are with strong hourly, weekly and annual seasonality. Table 4 presents the summary statistics for electricity gross load, i.e. from both eastern and western hubs over the period of April 1, 2002 to December 31, 2003. Mean values of the load are bigger than median values. Demand for peak afternoon hours tend to be higher and more volatile than for other hours. Figure 8 displays that summer demand is more volatile than winter demand. Moreover, average summer load is higher than average winter load.

Finally, the weather data is collected from the National Weather Station. The data on weather conditions are represented by temperature for PJM East (Philadelphia) and PJM West (Pittsburgh). Electricity load and weather conditions are used as explanatory variables in the economic model constructed in next section.

**PRICE MODELING**

The PJM Interconnection is divided into twelve transmission zones controlled by independent companies. Both real time and forward prices are given hourly for each of the twelve transmission zones. All zones act as independent markets, although they are tightly related through the constraints imposed by the transmission lines. These interconnections allow implementation of a spatial econometric approach to model price formation process in the PJM interconnection. Electricity is not a simple good; it complies only with the laws of physics. For instance, one cannot control the distribution of electricity in a network but only predict it using Kirchhoff’s Current Law. Knowing the features of a network allows one to identify flows but one can control them only by changing either the network or initial conditions. As a result, what is observed at one point is determined (in part at least) by what happens elsewhere in the system. This can formally be expressed as a spatial process:

\[
LMP_j = f(LMP_1, LMP_2, \ldots, LMP_N)
\]

Every observation of a variable \( LMP \) at location \( j \) is formally related to the magnitudes for the LMP variables in other spatial units in the system through the function \( f \). By imposing a particular form for the spatial process, i.e. on the functional relationship \( f \), a number of characteristics of the spatial dependence may be estimated and tested empirically. One approach to infer an appropriate form for the spatial dependence departs from the data and is based on a number of statistical indicators. The crucial issue in spatial econometrics is the problem of formally expressing the law in which the structure of spatial dependence is to be incorporated in the model. The first question of spatial dependence is the need to determine which other units in the spatial system have an influence on the unit under
consideration. Formally, this can be expressed most simply in the topological notion of nearest neighborhood. Spatial autocorrelation is based on the notions of binary contiguity between spatial units. If two spatial units have a common border of non-zero length they are considered to be contiguous. In the case of PJM interconnection there is no contiguity among some zones. For instance, zone APS is not coherent itself, and it is composed of two geographically isolated areas (see FIG 9). This fact impedes application of a spatial model. However to circumvent this obstacle, I treat each isolated geographical area as a zone. This approach simplifies the modeling without impairing the results. At the core of the locational marginal pricing model is the fact that prices are set to equate supply and demand and are the same across all zones unless there is transmission congestion. If at least one transmission line is congested, the LMPs are different across zones. So, treating 16 PJM’s geographical areas as independent zones can help to resolve non-contiguity problem.

For each area I specify the following regression equation:

$$S_{it} = \alpha_0 + \alpha_1 \cdot \text{weather}_{it} + \alpha_2 \cdot \text{forward}_{it} + \alpha_3 \cdot \text{load}_{it} + \sum_{j=1}^{23} \beta_{j}^i H_{jt} + \sum_{l=1}^{6} \beta_{l}^i W_{lt} + \sum_{k=1}^{24} \gamma_{k} S_{i,t-k} + \varepsilon_{it} \quad (1)$$

$$t = 1, \ldots, T; \quad i = 1, \ldots, N,$$

$$N = 16 \text{ and } T = 15336$$

$S_{it}$ stands for a spot price of zone $i$ at time $t$;

$\text{forward}_{it}$ is a forward price for delivery at date $t$ to zone $i$ contracted 24 hour earlier;

$\text{load}_{it}$ is a load at date $t$ for $i$ zone. Since PJM interconnection is divided into 2 independent areas: PJM-West and PJM-East, all zones are either in PJM-West or in PJM-East. So, those zones in PJM-East have the same load.

$\text{weather}_{it}$ is a temperature observed at zone $i$ at time $t$.

$H_j$ is an hour dummy (12 pm dummy is omitted)

$W_l$ is a week dummy (Sunday dummy is omitted)

$S_{i,t-1}$ is a spot price of zone $i$ at time $t-1$ (to capture intra-day seasonality as well as reduce non-stationarity)

Spatial dependence can arise from latent variables that are spatially correlated. It seems likely that unobserved characteristics such as line congestion, generating unit production capacity, generating plant maintenance problems at certain locations, and the like may exhibit spatial dependence. The most plausible model that may capture most of latent spatial correlation is Spatial Error Model (SER)

$$S = \beta X + \varepsilon \quad (2)$$
\[ S = (S_1, S_2, \ldots, S_{16})^T, \] where each \( S_i \) is a 15336\times 1 \) vector-column,

\[ X \text{ is } (15336 \times 16) \times 57 \text{ matrix, and } \varepsilon \text{ is } (15336 \times 16) \times 1 \text{ vector-column} \]

\[ \varepsilon = \lambda \Omega \varepsilon + u \quad (3) \]

where \( \Omega \) is known as a normalized row-stochastic matrix, \( \lambda \) is a scalar coefficient of spatial correlation in errors. It captures the underlying structure of neighboring zones by “0-1” values. That is, if two zones have a common border of non-zero length a value of 1 is assigned. For any two neighboring zones \( i \) and \( j \), I assume that area \( j \)’s explanatory variables do not correlate with error term of area \( i \).

For \( T \) spot prices in \( N \) zones, \( \Omega \) is a \((NT \times NT)\) weighting matrix that assigns to spot price in the area \( j \) the average value of variable \( S \) in the areas surrounding the area \( j \). In this model all neighbors are given equal weight, and all areas are equally influenced by their neighbors taken together (sum of elements in each row of \( \Omega \) is unity). These assumptions may be relaxed if more information about the relative importance of neighboring zones is available.

The error term \( \varepsilon \) has two components. The vector \( u \) is a \((NT \times 1)\) vector of random errors with zero mean, constant variance and no correlations to the explanatory variable, i.e. \( E(u) = 0, \operatorname{VAR}(u) = \sigma_u^2 I \) and \( E(X'u) = 0 \). A spatial error term, \( \lambda \Omega \varepsilon \), can be interpreted as the following: the error terms for observations in any area \( j \) contain \( \lambda \) times the average error found in neighboring areas, \( \Omega \varepsilon \). Spatial correlation in errors, \( \lambda \neq 0 \), may result when unobserved spatially correlated variables drive prices, such as grid topology and physical characteristics of the transmission lines. Any unobserved regional differences may result in unobserved errors being different in different areas, but related in surrounding areas.

For a model with an error structure as in (3), ordinary least squares estimation is inefficient. If OLS is performed ignoring the spatial structure of errors the estimates of \( \beta \) are still unbiased, but the estimates of variance are biased and may lead to spurious inference. Therefore, maximum likelihood estimation is used. The results of estimating the spatial autoregressive error model are represents in TABLE 0. The SEM estimates indicate that after taking into account the influence of the explanatory variables, we still have spatial correlation in the residuals of the model because the parameter \( \lambda \) is significantly different from zero. As a confirmation of this, consider the results from an LR test:
Recall that this is a test of spatial autocorrelation in the residuals ($H_0$ is of no spatial correlation) from a least-squares model, and the test results provide a strong indication of spatial dependence in the least-squares residuals. Note also that this is the only test that can be implemented successfully with large data sets.

Observing the reported results in Table 0, one can draw several conclusions. The information about the load and the forward prices captures much of the variation in real time prices. The first explanation of this fact is that day-ahead commitments are done to mitigate risk associated with real-time uncertainty. Therefore, the real time LMPs are, in a sense, predetermined by day-ahead contracts. In addition, load represents demand, which actually determines generation, and in turn, spot prices. Even though load is only an approximation of demand, one can treat it as an upper bound for demand, since it impossible to consume more than it is produced. Thus, load may explain spot prices fairly well.

The estimates of the $H_j$ and $W_k$, hourly and weekly dummies, are included in order to capture the intra-day and weekly seasonality. The estimates of hourly dummy variable coefficients are all significantly positive except $H_3$, whereas the estimates of weekly dummy are all significantly negative. This captures the weekly cyclical pattern in spot prices due to variations in residential, commercial and industrial use. Electricity prices tend to increase from early morning until late afternoon, and tend to decrease until midnight. Moreover, electricity spot prices are lower in weekends than on weekdays, as is reflected in the dummy variables estimates.

The estimates of the lagged electricity spot prices have even more intriguing behavior. Most of the even-hour dummies are negative, whereas most of the odd-hour dummies are positive. The only exceptions are the dummies for lagged spot prices from 18 till 24, which are all positive and significant except the dummy for lag 20. The other insignificant estimates for hour dummies are lags for 8, 9, 13 and 17. The insignificance of hour dummies can be driven by the fact that the variables “weather” and “load” are included into the model. These variables capture the great portion of the spot prices changes. Another explanation to this can be the fact that electricity spot prices are highly volatile. This non-stationarity in the prices may cause the result.
There is a significant estimated “spatial” parameter $\hat{\lambda}$ which means that there is strong spatial correlation in the residuals. The main message is that spatial dependence of spot prices in the PJM market is important and one should not ignore this spatial correlation, even though it is driven by unobserved (to the researcher) processes. The best way to circumvent the spatial unobserved factors is to model them as a specific error process. This can be done in several ways: accounting for the topology of the network or assuming spatial process in disturbances. In any case, the spatial characteristics of the electricity market should be taken into account while modeling the electricity prices and their derivatives. Although the coefficient $\hat{\lambda}$ is considered to be a nuisance parameter, usually of little interest in and of itself, it is necessary to correct for or filter out the dependence. It is worth noticing than since $E(u) = 0$, irrespective of the value of $\hat{\lambda}$, the mean of $S$ is not affected by the spatial error dependence.

**Figure 4: Spatial Regression Residuals**

In Figure 4, the residuals appear to exhibit a white noise pattern, even though there are several outliers, which are associated with July 2002 spikes in the spot prices. As can be seen in the next Figure 5, those spikes are underestimated. Note, that on the horizontal axes time series for all 16 zones are represented. Overall performance of the Spatial Error model is satisfactory, since it bring new insight into the electricity price modeling and help to estimate those prices well.
CONCLUSION

Spatial Error Correction model is adequate to model electricity prices. The problem of unobserved spatial correlation in the grid can be modeled by the SEM. The model provides an additional insight about the spot electricity prices in the PJM market. The topology of the network, the structure of the market and the rules imposed are responsible for the spatial correlation, which should not be ignored by careful research. Strong spatial correlation is supported by the estimating results as well as by the testing procedure. Though the estimation of the “spatial” parameter \( \lambda \) is of little interest, it helps to bring out consistent estimates of explanatory variables. Therefore, the more robust estimates and inference can be drawn.

Despite its attractiveness, the Spatial Error Model is not the only method available to model the electricity prices and derivatives. Future of electricity price modeling may be oriented towards models incorporating finer components and an additional information about the network topology, weather conditions and connections between the PJM zones. The additional information can be utilized either by spatial approach or by other modeling methods.
# TABLE 0 EMPIRICAL RESULTS

<table>
<thead>
<tr>
<th>Variable Description</th>
<th>Coefficient</th>
<th>t-stat</th>
<th>z-probability</th>
<th>Variable Description</th>
<th>Coefficient</th>
<th>t-stat</th>
<th>z-probability</th>
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<td><strong>LAMBDA - coefficient of spatial</strong></td>
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<td>-3.04175</td>
<td>0.002352</td>
<td><strong>W3</strong></td>
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**R-squared** = 0.9575  
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**Rbar-squared** = 0.9575  
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REFERENCES


## APPENDIX

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FIG. 6 Time series of average over zones electricity spot prices ($/MWh)

FIG. 7 Time series of average over zones day-ahead electricity prices ($/MWh)
FIG. 8  TIME SERIES OF ELECTRICITY LOAD (1000'S MW).

FIG. 9 PJM TRANSMISSION ZONES TAKEN FROM PJM WEB-SITE